# Theoretical Evaluation of Maximum Doping Concentration, Breakdown Voltage and On-state Resistance of Field-Plate Compensated Devices

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## Abstract

The idealised on-state resistance vs. breakdown voltage behaviour for field-plate compensated devices is analysed for different impact ionisation models. For small device dimensions, we found a significant deviation from common values of maximum doping concentration due to an overestimated impact ionisation coefficient at higher electric fields. This, in turn, leads to a lower doping density and higher on-state resistance compared to the optimal values.

Keywords: MOSFET, Electric Field, Impact Ionisation, Charge Compensation

# INTRODUCTION

Several structures to overcome the unipolar silicon limit have been proposed in recent years. The well-known CoolMOS<sup>TM</sup> device for example represents superjunction devices, where the n-drift region donors are compensated by acceptors located in p-columns as schematically shown in Fig. 1. Super-junction devices are available for blocking voltages in the range of 500 V to 900 V.

For low-voltage devices, the oxide-bypassed or fieldplate structure is more advantageous. Here, an isolated field-plate provides the necessary charges to compensate the drift region donors as illustrated in Fig. 2. The idea here is to divert the electric field lines such that the number of field lines passing through any location is minimized. The deviation of field lines requires additional charges somewhere else to allow field lines in the space-charge region to originate or terminate there. The field-plate provides such compensation charges, hence the name "compensation



Fig. 1: Compensation of positive donor charges in n-doped columns by negative acceptor charges located in p-doped columns

principle".

The on-state resistance of the device is mainly determined by the doping concentration in the mesa region. The design of such devices cannot be accomplished without sophisticated device simulation tools due to the inherent two-dimensional effects. Nevertheless, analytical models provide a better insight into the nature of the underlying effects and serve as a good starting point for device simulation.

## **DEVICE STRUCTURE**

We shall restrict ourselves to the basic structure as shown in Fig. 3. This device structure, as presented e.g. in [1-4], is referred to as a field-plate structure or as an oxide-bypassed structure.

The main parameters are the uniform doping concentration  $N_D$  in the mesa or drift region, the mesa width w, the mesa length L and the oxide thickness  $t_{\rm ox}$ . Complete compensation is achieved if the entire mesa region is depleted, that is if the space charge width  $w_{\rm SC}$  is half the mesa width.



Fig. 2: Compensation of the positive donor charges in the nregion by negative charges located on the isolated field-plates in the trenches



Fig. 3: Basic structure of field-plate compensated devices

# IMPACT IONISATION MODELS

The doping in the mesa region determines the on-state resistance and simultaneously the achievable breakdown voltage. To analyse the behaviour of the previously introduced structure, thorough theoretical analysis has been carried out in recent years [4].

Breakdown occurs if the electric field becomes larger than the critical electric field  $E_{crit}$ , which depends on the length of the space-charge region (SCR)  $w_{sc}$ .  $E_{crit} = f(w_{sc})$ is the electric field that causes the ionisation integral to become unity. For electrons, the integral is given by [5]:

$$I_{ava} = \int_{0}^{w_{sc}} \alpha_{n} \cdot e^{\int_{x}^{w_{sc}} (\alpha_{p} - \alpha_{n}) dx'} dx, \qquad (1)$$

where  $\alpha_n$  and  $\alpha_p$  are the ionisation coefficients for electrons and holes, respectively. A similar expression holds valid for holes:

$$I_{ava} = \int_{0}^{w_{sc}} \alpha_{p} \cdot e^{0} dx' dx .$$
 (2)

Fig. 4 shows the dependence of the ionisation integral



A further simplification is possible if an effective impact ionisation coefficient  $\alpha_{eff}$  can be derived. An accurate calculation of the breakdown voltage can be done as long as the relation  $\alpha_n / \alpha_p$  is independent of the electric field and thus a constant [9-11]. If this assumption is valid in the investigated range of the electric field, the effective impact ionisation coefficient is given by:

$$\alpha_{\rm eff}(E) = \frac{\alpha_{\rm n} - \alpha_{\rm p}}{\ln\left(\frac{\alpha_{\rm n}}{\alpha_{\rm p}}\right)}.$$
(3)

For the ease of calculations, a polynomial approach for the dependency of the effective ionisation coefficient on the electric field E was proposed by Fulop [12]:

$$\alpha(\mathbf{E}) = \boldsymbol{\beta} \cdot \mathbf{E}^{\,7} \,. \tag{4}$$

Eq. 4 is widely used for analytical investigations of power device breakdown capability due to its simplicity. For the expression of Fulop with  $\alpha_n \approx \alpha_p \approx \alpha_{eff}$ , the avalanche integral reduces to:

$$I_{ava} = \int_{0}^{w_{sc}} \alpha_{eff} \, dx \,. \tag{5}$$

Yet, for smaller device dimensions, this assumed dependency is no longer accurate. Under these conditions, the critical electric field is higher than that predicted by the polynomial approach of Fulop. A better approximation is given in several impact ionisation



Fig. 4: Impact ionisation integral for electron-induced and hole-induced avalanche process



Fig. 5: Impact ionisation coefficients as function of the electric field



Fig. 6: Critical electric field as function of ionisation length

models intended to be used in device simulation programs.

A comparison of the effective impact ionisation coefficient  $\alpha_{eff}$  as proposed by Fulop [12] and the electron impact ionisation coefficients  $\alpha_n$  as given by several impact ionisation models [6,9,13] is provided in Fig. 5. It is clear that Fulop's model differs significantly from these more advanced approaches for electric fields higher than  $E = 4 \cdot 10^5$  V/cm.

Instead, the model proposed by Valdinoci [6] is used since it also delivers a better temperature dependency compared to other models [14]. Here, the ionisation coefficients depend on the electric field as follows:

$$\alpha(E) = \frac{E}{a(T) + b(T) \exp \frac{d(T)}{E + c(T)}},$$
(6)

with the temperature dependent parameters a,b,c and d. Application of Eq. 5 to Fulop's model and Eq. 1 to Valdinoci's model is shown in Fig. 6. A significantly higher critical electric field is observed at small dimensions for Valdinoci's model.

Despite the obvious deviations, Fulop's model still is eligible since it allows analytical investigations of impact ionization phenomena while in case of Valdinoci's model a numerical solution is used.

#### ANALYTICAL MODEL

#### The 1D- Capacitor

In a first approach, the field-plate oxide stack can be approximated by a capacitor. The voltage across this capacitor is given by:

$$V_{cap} = \frac{Q}{C} = q \cdot N_D \cdot \frac{w}{2} \cdot \frac{t_{ox}}{\varepsilon_0 \cdot \varepsilon_{ox}}, \qquad (7)$$

It is assumed that the mesa region is completely depleted by this voltage and that the charge is solely located at the Si/Si0<sub>2</sub>-interface.

A constant mesa doping gives rise to a triangular horizontal electric field. As a result, the maximum possible voltage drop  $V_{wsc}$  in the space-charge region is given by:

$$V_{\rm wsc} = \frac{\varepsilon_0 \cdot \varepsilon_{\rm Si} \cdot E_{\rm crit}^2}{2 \cdot q \cdot N_{\rm D}}.$$
 (8)

with the critical electric field  $E_{\rm crit}$  for a given doping concentration and space-charge extension  $w_{\rm sc}.$ 

The applied total voltage  $V_{total}$  can be divided into a voltage  $V_{cap}$  across the oxide region (capacitor) and a voltage  $V_{wsc}$  across the silicon region (mesa) which is important for the breakdown. Their relation can be approximated by a voltage distribution factor:

$$\Theta = \frac{V_{cap}}{V_{wsc}} \,. \tag{9}$$

Eliminating V<sub>wsc</sub> gives

$$\Theta = \frac{V_{cap} / V_{total}}{V_{wsc} / V_{total}} = \frac{V_{cap} / V_{total}}{1 - V_{cap} / V_{total}} .$$
(10)

The maximum doping concentration in the compensation region can then be obtained from Eq. 7 and Eq. 8 as a function of the critical electric field  $E_{crit}$ :

$$N_{D,max} \le 10^4 \sqrt{\Theta} \frac{\varepsilon_0}{q} \sqrt{\frac{\varepsilon_{Si} \cdot \varepsilon_{ox}}{2}} \cdot \frac{E_{crit}}{\sqrt{\frac{W}{2} t_{ox}}} cm^{-3} ,(11)$$

with w/2 and  $t_{ox}$  in  $\mu m,~\epsilon_0$  = 8.85  $\cdot 10^{\cdot 14}$  F/cm and  $E_{crit}$  in V/cm.

From Eq. 11 it can be concluded that in general a higher doping is allowed for smaller device dimensions. It can be seen from Fig. 6, that in case of Valdinoci's model an even larger critical electric field is predicted for decreasing mesa width. For small device dimensions, the higher critical electric field and the smaller



Fig. 7: Comparison of the maximum doping concentration in the drift region for different impact ionisation models as a function of device dimensions ( $t_{ox} = 0.5 \ \mu m, \Theta = 2$ )

ionisation coefficient leads to a higher allowed maximum doping density if the model of Valdinoci instead of Fulop is used. This result is shown in Fig. 7. The model employing the impact ionisation rates in accordance with the model of Valdinoci is sufficient to determine the maximum doping concentration which is allowed in the device. Unfortunately, this does not provide any information on the breakdown voltage.

Applying the relation  $E_{crit} \propto N_D^{-1/8}$  of [15] to Eq. 11 under the assumption of  $\Theta = 1$  gives the well-known relationship derived in [4]:

N<sub>D,max</sub> = 
$$1.07 \cdot 10^{16} \left(\frac{W}{2} t_{ox}\right)^{-\frac{4}{7}} cm^{-3}$$
, (12)

with w/2 and  $t_{\text{ox}}$  in  $\mu m.$ 

t<sub>ox</sub>

#### The 1D - Field-Plate - MOS System

A more sophisticated model of the structure can be seen in Fig. 8. It generally resembles a simple MOS capacitor, with the exception that no inversion layer can build up because any mobile carriers are removed by the electric field component parallel to the interface. This is taken into account in the capacitor model in Fig. 8 by considering the fixed space charges only, thereby permitting a simple derivation of the electrostatic potential  $\varphi$  and the electric field E. The latter is constant in the oxide:

$$E_{ox} = \frac{\phi(0)}{2}$$
.

The electric field in the silicon at the Si/SiO<sub>2</sub> interface is, with  $\eta = \epsilon_{ox} / \epsilon_{Si}$  (neglecting interface charges):

$$\mathbf{E}(\mathbf{0}) = \boldsymbol{\eta} \cdot \mathbf{E}_{\mathbf{0}\mathbf{X}} \tag{14}$$

Incorporating the additional boundary condition



Fig. 8: The MOS-System modelling the field-plate structure



Fig. 9: Voltage distribution factor  $\Theta$  versus applied drain voltage of the MOS system with constant doping in which  $V_{DF}$  is the applied voltage between Drain (D) and field-plate (F).

$$E(w_{SC}) = 0 \tag{15}$$

into Poisson's equation for the given system leads to the electric field in the silicon

$$E(x) = -\frac{q N_D}{\varepsilon_0 \varepsilon_{Si}} x + \eta \frac{\phi(0)}{t_{OX}}, \qquad (16)$$

and the length of the space charge region

$$w_{SC} = \eta \frac{\phi(0)}{t_{OX}} \cdot \frac{\varepsilon_0 \varepsilon_{Si}}{q N_D}.$$
 (17)

Note the dependence on  $\varphi(0)$  which is obtained by integrating Eq. 16:

$$\varphi(0) = \frac{-1 + \sqrt{1 + 2 \cdot \xi \cdot V_{\text{DF}}}}{\xi}, \qquad (18)$$

with

(13)

$$\xi = \frac{\varepsilon_0 \cdot \varepsilon_{\rm Si} \cdot \eta^2}{t_{\rm ox}^2 \cdot q \cdot N_{\rm D}} \tag{19}$$

and the voltage between Drain and field-plate  $V_{DF}$ . Combining Eq. 17 - 19 finally gives:

$$w_{SC} = \frac{t_{ox}}{\eta} \left( -1 + \sqrt{1 + \frac{2 \cdot \varepsilon_0 \cdot \varepsilon_{Si} \cdot \eta^2}{t_{ox}^2 \cdot q \cdot N_D}} V_{DF} \right).$$
(20)

With these findings, Eq. 10 translates to

$$\Theta = \frac{\phi(0) / V_{\rm DF}}{1 - \phi(0) / V_{\rm DF}} \,. \tag{21}$$

A corresponding example plot for one doping concentration value and different oxide thicknesses in the range of interest can be seen in Fig. 9. It shows that the assumption of a constant voltage distribution factor  $\Theta$  should be restricted to a sufficiently small voltage range. Under this condition, a carefully chosen value of the voltage distribution factor  $\Theta$  allows a good estimation of the maximum doping concentration N<sub>D</sub> using Eq. 11.

# Calculation of breakdown voltage and drift resistance

Within a certain compensation length, the breakdown voltage remains constant [4]. The breakdown voltage in this case depends solely on the mesa width and the critical electric field according to Fig. 6:

$$V_{BD} = 1.8 \cdot 10^{-4} \cdot E_{crit} \left(\frac{w}{2}\right) \cdot \frac{w}{2} V, \qquad (22)$$

with  $E_{crit}$  in V/cm and w in  $\mu m$  [4].

The device dimensions and doping concentration determine the normalised on-state resistance of the drift zone  $R_{Drift}$ ·A with length L. It is given by:

$$R_{\text{Drift}} \cdot A = \frac{L}{q \cdot \mu_n(N_D) \cdot N_D} \left( 1 + \frac{t_{\text{ox}}}{w/2} + \frac{t_{\text{FP}}/2}{w/2} \right), (23)$$

with the doping dependent electron mobility  $\mu_n$  and the thickness of the field-plate  $t_{FP}$ . A higher doping concentration leads to a lower on-state resistance. However, mobility reduction sets in above a certain doping concentration. The doping concentration can be estimated by using Eq. 11 with a voltage distribution factor  $\Theta = 2$ :

$$N_{\rm D} = 10^4 \, \frac{\varepsilon_0}{q} \sqrt{2} \, \sqrt{\frac{\varepsilon_{\rm Si} \cdot \varepsilon_{\rm ox}}{2}} \cdot \frac{E_{\rm crit}}{\sqrt{\frac{w}{2} t_{\rm ox}}} \, {\rm cm}^{-3} \, . \tag{24}$$

In order to analytically determine the drift resistance  $R_{Drift}$ , the minimal drift region length as found in [4],  $L = 5 \cdot w / 2$ , is used. This makes it possible to relate the drift region resistance to the breakdown voltage  $V_{BD}$ .

# **DEVICE SIMULATION**

The simulation result of the dependency of the breakdown voltage  $V_{BD}$  on the drift region doping  $N_{D}$ for a given structure is shown in Fig. 10. Obviously, there is a maximum doping density leading to a maximum breakdown voltage V<sub>BD</sub>. Two regions can be distinguished. For doping concentrations to the left of the maximum, the breakdown is mainly pinned at the trench bottom, whereas for doping concentrations to the right of the maximum, the breakdown is located in the middle of the cell. The current paths are different in both cases. This can be seen from breakdown simulations as shown in Fig. 11. The avalanche breakdown location changes if the mesa region is not fully depleted at breakdown. This is the case on the right side of the maximum of the dependency shown in Fig. 10 (e.g. for large doping concentrations). The



Fig. 10: Simulated characteristics of breakdown voltage as function of drift region doping for a given structure.

increased doping in this region causes the potential to penetrate deep into the mesa region towards the groove contact. The curvature of the equipotential lines is proportional to the doping concentration in the mesa region. If the doping concentration becomes too high, the width of the SCR reduces and drops below half the mesa width. If this happens, any small additional reduction will move the potential lines deeper into the mesa region and the field-plates will increasingly lose their ability to laterally compensate the mesa region. The breakdown voltage  $V_{BD}$  further depends on the



Fig. 11: Location of breakdown for

a) high doping of drift region (right side of maximum)b) low doping of drift region (left side of maximum)Contours are impact ionisation rates (dark colours are high values) while the flowlines indicate the current path.



Drift region length L

Fig. 12: Determination of drift region length for the calculation of the drift region resistance

length of the compensation region, i.e. the trench depth [4].

For comparison with the simple analytical model, simulations like the ones shown in Fig. 10 were performed for a large number of structures. Variations included drift region doping N<sub>D</sub>, mesa width w, mesa length L and oxide thickness tox (cf. Fig. 3). Simulations were extended to further investigate the influence of the compensation region length on the breakdown voltage and the drift-region resistance. In a first step, the doping density was varied for a given geometry to find the doping value corresponding to the maximum breakdown voltage. In a second step, the drift region length (and therefore the trench depth) was decreased until the change in the breakdown voltage started to show a significant reduction as qualitatively explained by Fig. 12. Thus for each given geometry, determined by a oxide thickness  $t_{\text{ox}}$  and a mesa width w, a maximum breakdown voltage  $V_{\text{BD}}$  and an optimal drift region length L with its corresponding drift region resistance R<sub>Drift</sub> is found.

In all simulations, the thickness of the field-plate  $t_{\rm FP}$  was kept constant.

# **RESULTS AND COMPARISON**

Fig. 13 shows the dependence of the drift region resistance on the maximum gained breakdown voltage. Here, a comparison is given between:

- the model introduced in this work
- the relation found by Chen in [4]
- the 2D simulation results
- the 1D silicon limit [16]

Considering a more realistic dependence of the critical electric field on small dimensions obviously leads to a considerably smaller drift region resistance in comparison with the model presented in [4]. In contrast to these results it can now be concluded that field-plate compensated structures are also an advantageous alternative for low-voltage devices. This result of the



Fig. 13: Drift region resistance vs. breakdown voltage for different models

simple 1D model is also supported by the 2D simulation results. Here, even lower values for the drift region resistance are found.

# CONCLUSION

For power MOSFETs in the voltage range below 300 V, the application of charge compensation principles leads to structures employing field-plates. These field-plate or oxide-bypassed structures allow the unipolar silicon limit to be overcome.

In this work, the relationship between breakdown voltage and drift region resistance is analysed for such devices. In contrast to similar investigations published elsewhere, a more realistic model for the dependence of the critical electrical field on the ionisation length was considered. This proved to be necessary due to the small device dimensions usually present in the structures of interest and is especially important for devices with low breakdown voltages.

Due to the limitations of the simple 1D model, a voltage distribution factor is introduced. It is shown that this distribution factor is constant within a certain parameter range which allows an estimation of the main parameters of the device.

The results of 2D device simulations, which are not affected by the limitations of the simple 1D model, support the validity of the analytic estimation although lower values of the drift resistance were calculated.

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